

Can show soundness and completeness theorem for 1st order logic i.e., $\Gamma \models F$ iff $\Gamma \vdash F$ Gödel '30

How to make a theorem prover for 1st order logic.

Basic Idea: Want to reduce to propositional case.

- ① Convert using some of operation previously described
 formulas ^{in KB and to be proven} to prenex normal form

$$\forall \vec{x} \exists \vec{y} \forall \vec{z} \dots G(\vec{x}, \vec{y}, \vec{z}, \dots)$$

where G does not quantifiers

- ② Introduce f^n symbols for $\forall \exists$ pairs

$$\exists x \forall y G(x, y) \Rightarrow G(x, f_1(x), \dots, f_n(x))$$

$\vec{y} = y_1 \dots y_n$

- ③ Once get open formula ~~to~~ convert to CNF and try to use resolution algorithm.

What is different b/w 1st order resolution and propositional resolution?

Now need a concept called unification

EX) $\text{num}(0)$ \leftarrow now have to match f^n symbols
 $\text{num}(S(X)) : -\text{num}(X)$

!? $-\text{num}(S(S(0)))$

returns true

!? $-\text{num}(X)$