

Statistical Learning Methods

Idea given some data (evidence) and have some hypotheses of how the data works, would like to do,

- 1) Choose most likely hypothesis to explain the data
- 2) Predict future data

Example: Bags of candy which can be 1 of 5 types.

- h1: 100% cherry
- h2: 75% cherry 25% lime
- h3: 50% cherry 50% lime
- h4: 25% cherry 75% lime
- h5: 100% lime

$$H = \{h_1, \dots, h_5\}$$

Candy chosen from bag revealed one at a time

D_1, \dots, D_n Each d_i is a random variable

Bayesian Learning

Idea calculate probability of each hypothesis given the data and make a prediction of next item.

D – space of all data sets

d – a vector of observed values from **D**.

Example: <cherry, cherry, lime, ...>

Probability of a given hypothesis

$$p(h_i | \mathbf{d}) = \frac{p(\mathbf{d} | h_i) p(h_i)}{\alpha} \quad (\alpha \text{ is normalization factor})$$

company might tell us that $p(H) = \langle .1, .2, .4, \dots \rangle$

Say we have $p(h_i | \mathbf{d})$ then calculate probability of next candy as:

$$p(X | \mathbf{d}) = \sum P(X | h_i) P(h_i | \mathbf{d})$$

How to calculate $P(\mathbf{d} | h_i)$:

$$P(\mathbf{d} | h_i) = \prod P(d_i | h_i)$$