

Quadrics et al

CS116B

Chris Pollett

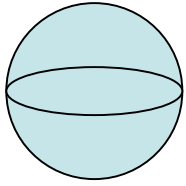
Jan 31, 2005.

Outline

- Quadric Surfaces
- SuperQuadrics
- OpenGL

Quadrics Surfaces

- Quadrics are a frequently used class of surfaces.
- They include spheres, ellipsoids, torii, paraboloids, and hyperboloids.
- They get their name because they are described by second degree equations.



Spheres

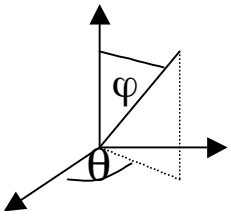
- The sphere of radius r can be described as those points satisfying the equation: $x^2+y^2+z^2=r^2$. (non-parametric equation)
- It can also be described as those points satisfying:

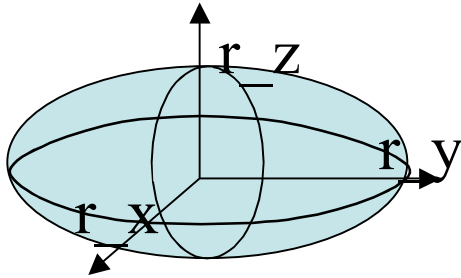
$$x(\varphi,\theta) = r*\cos \varphi*\cos \theta, \quad -\pi/2 \leq \varphi \leq \pi/2$$

$$y(\varphi,\theta) = r*\cos \varphi*\sin \theta, \quad -\pi \leq \theta \leq \pi$$

$$z(\varphi,\theta) = r*\sin \theta$$

I wrote x,y,z as above to emphasize we have a mapping from (φ,θ) to $(r*\cos \varphi*\cos \theta, r*\cos \varphi*\sin \theta, r*\sin \theta)$





Ellipsoid

- Can view as a squashed sphere.
- More, formally, we have three radii: r_x , r_y , r_z and the ellipsoid is described by those points satisfying:

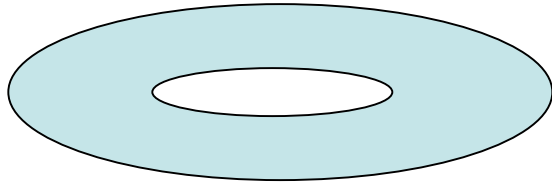
$$(x/r_x)^2 + (y/r_y)^2 + (z/r_z)^2 = 1.$$

- A sphere is an ellipsoid where $r_x=r_y=r_z$.
- The parametric equations for an ellipsoid are:

$$x(\varphi, \theta) = r_x \cos \varphi \cos \theta, \quad -\pi/2 \leq \varphi \leq \pi/2$$

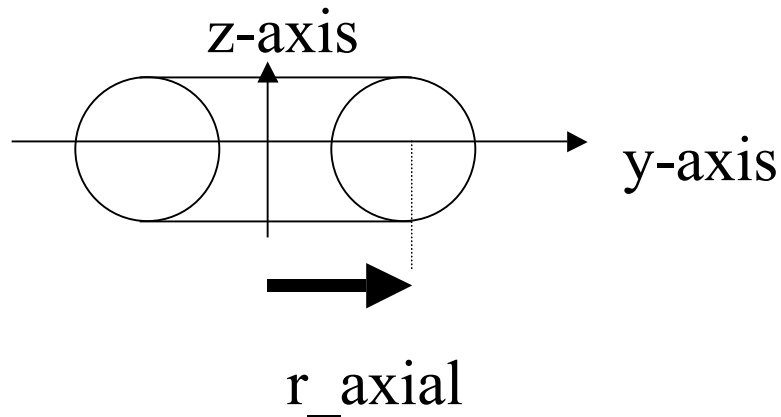
$$y(\varphi, \theta) = r_y \cos \varphi \sin \theta, \quad -\pi \leq \theta \leq \pi$$

$$z(\varphi, \theta) = r_z \sin \theta$$



Torus

- Basically, a fancy word for a doughnut
- Can make a torus by rotating a circle along a perpendicular circle of some fixed radius:



- One can do this with the equations:

$$(y-r_{\text{axial}})^2+z^2=r^2 \text{ or } x=(r_{\text{axial}}+r*\cos \varphi)*\cos \theta, y=(r_{\text{axial}}+r*\cos \varphi)*\sin \theta, z=r*\sin \varphi.$$

SuperQuadratics

- These are generalizations of quadrics.
- We add some additional parameters to the quadric equations which allows us to tweak the basic shapes.
- The equations will generally not be quadratic in these new parameters.

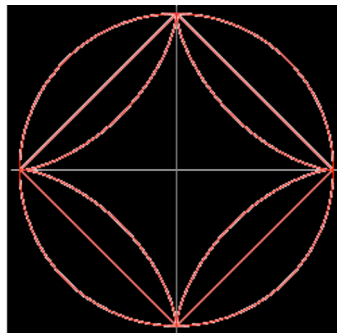
Superellipse

- A superellipse (a 2D object) is given by the equation:

$$(x/r_x)^{2/s} + (y/r_y)^{2/s} = 1 \text{ or}$$

$$x = r_x \cos^s \theta, y = r_y \sin^s \theta$$

- Figure below shows different $s \geq 1$



Superellipsoid

- A superellipsoid is a generalization of a superellipse to 3D.
- Equations are:

$$[(x/r_x)^{2/s-2} + (y/r_y)^{2/s-2}]^{s-2/s-2} + (z/r_z)^{2/s-1} = 1$$

or

$$x = r_x * \cos^{s-1} \varphi * \cos^{s-2} \theta,$$

$$y = r_y * \cos^{s-1} \varphi * \sin^{s-2} \theta,$$

$$z = r_z * \sin^{s-1} \varphi$$

GLUT Quadrics

- We now discuss how to draw quadrics using GLUT.
- To begin, for spheres the functions are:
 `glutWireSphere(r, nLongitudes, nLatitudes);`
 or
 `glutSolidSphere(r, nLongitudes, nLatitudes);`
- Obviously, `r` is the radius (it is a double)
- `nLongitudes` is the number of circles through both poles to be used in the sphere.
- `nLatitudes` is the number of circles parallel to the equator to be used in the sphere.

More Glut Quadrics

- Cones can be drawn with:
 `glutWireCone(rBase, height, nLongitudes, nLatitudes);`
 or
 `glutSolidCone(rBase, height, nLongitudes, nLatitudes);`
- Torii can be drawn with:
 `glutWireTorus(rCrossSection, rAxial, nConcentrics, nRadialSlices);`
 or
 `glutSolidTorus(rCrossSection, rAxial, nConcentrics, nRadialSlices);`
- `rCrossSection` is the `r` of before, `rAxial` is `r_axial`.
- `nConcentrics` - num circles centered on z axis. `nRadialSlices` -circles used in the axial rotation

Famous GLUT Surface

- One of the first surfaces to be modeled (by hand) as a polygon mesh in a computer graphics system was a teapot (Martin Newell 1975).
- This teapot still exists and can be drawn using:
`glutWireTeapot(size);` or `glutSolidTeapot(size);`

GLU Quadrics

- GLU provides slightly more flexible functions for drawing quadrics.
- Basic sequence of calls looks like:

```
GLUquadric *sphere1;  
sphere1 = gluNewQuadric();  
gluQuadricDrawStyle(sphere1, GLU_LINE); // wireframe  
gluSphere(sphere1, r, nLongitudes, nLatitudes);
```
- Some draw styles are `GLU_POINT` (just points), `GLU_SILHOUETTE` (wireframe less shared edge for coplanar facets) and `GLU_FILL` (like solid)

More GLU Quadrics

- Some other quadrics available are:
 - `gluCylinder(name, rBase, rTop, height, nLongitudes, nLatitudes);`
 - `gluDisk(name, rInner, rOuter, nRadii, nRings);`
//can use for flat disks with or without a hole
 - `gluPartialDisk(name, rInner, rOuter, nRadii, nRings, startAngle, sweepAngle);`

More GLU Quadric functions

- Once we are done with a quadric we can reclaim its memory with:

```
gluDeleteQuadric(name);
```

- We can define the front and back direction for the facet's normal vectors with:

```
gluQuadricOrientation(name, normalVectorDirection);
```

```
//GLU_INSIDE
```

```
//GLU_OUTSIDE
```

```
gluQuadricNormals(name, generationMode);
```

```
// GLU_NONE, GLU_FLAT, GLU_SMOOTH.
```

- Finally, we can define a callback that is called if an error occurs during the draw of the quadric with:

```
gluQuadricCallback(name, GLU_ERROR, function);
```