

# Physical Modeling and Surface Detection

CS116B

Chris Pollett

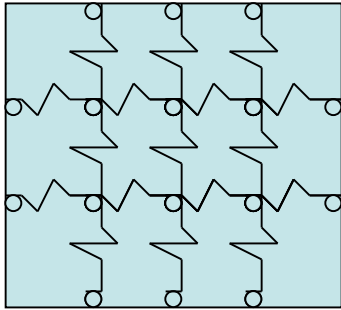
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# Outline

- Particle Systems
- Physical Modeling and Visualization
- Classification of Visible Surface Detection Algorithms
- Back Face Detection
- The Depth Buffer Method

# Particle Systems

- It is often useful to describe an object as a collection of disjoint pieces.
- Such an object is called a *particle system*.
- Particle systems can be useful for modeling things like smoke, fluids, explosions, grass, etc.
- As an example, to create fireworks, start with a collection of particle spheres drawn at some single fixed point. Shoot the particles out from this point in different, random directions and add gravity.



# Physical Modeling

- Non-rigid objects, such as rope, cloth, etc, can be modeled with physically based modeling techniques.
- For instance, a cloth might be modeled as a grid of mass points connected by strings.
- Force equation for such a spring given  $F = kx$ . Can model how mass points move when other forces like gravity are applied. Then one can texture map polygons faces of grid of mass points to draw the final object.

# Visualization of Data Sets

- Scalar Fields -- function from several dimensions into one. For example,  $f(x,y)$  or  $f(x,y,z)$ .
  - To draw  $f(x,y)$  can use elevation grid
  - To draw  $f(x,y,z)$  can use pseudo-color methods and assign ranges of values for field different color values.
  - To draw can use contour plots of  $f(x,y) = c$  or  $f(x,y,z) = c$  for different  $c$ 's. 2D-case gives isolines; 3d case gives iso-surfaces.

# Representing Vector Fields

- Functions which take a vector and return a vector.
- $\mathbf{F}(x,y,z)$  or  $\mathbf{F}(x,y)$ .
  - can draw lines and arrows attached to points  $(x,y,z)$ , or  $(x,y)$ .
  - Can use field lines

# Representing Tensors

- A tensor of type  $(p, q)$  on  $\mathbb{R}^n$  takes  $p$  row vectors of length  $n$  and  $q$  column vectors of length  $n$  and outputs a scalar. Alternatively, can think of as taking  $q$  column vectors and outputting  $p$  row vectors of length  $n$ . Map must be linear in each argument.
- Used in talking about materials (stress tensor), fluid dynamics, relativity, etc.
- To draw one can output tensor contractions of the tensor or can use different colored scalar or vector representations superimposed on the same scene.

# Classification of Visible Surface Detection Algorithms

- Algorithms for determining which surfaces would be visible on the screen can be broken into two broad categories:
  - Object space methods -- these compare objects or parts of objects to figure out who is in front of who.
  - Image space methods -- these compute visibility point by point at each pixel value on the projection plane.



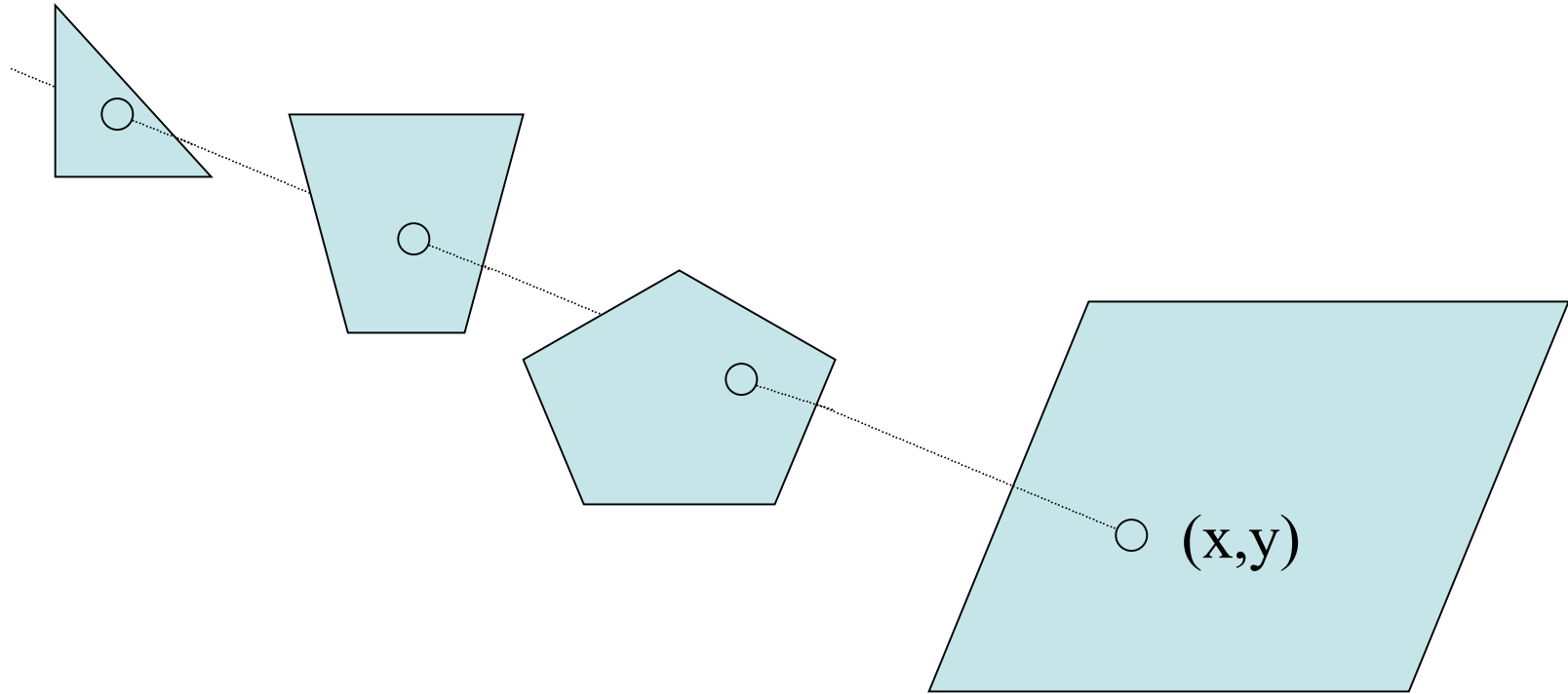
# Back Face Detection

- A point  $(x,y,z)$  is said to be behind a polygon surface if  $Ax + By + Cz + D < 0$  where  $A,B,C,D$  determine the plane of the polygon.
- If this point is along the line of sight to the surface, then we must be looking at the back of the polygon.
- Said another way, if  $\mathbf{N}$  is the normal to the polygon and  $\mathbf{V}_{\text{view}}$  is the viewing vector from the camera position, then the polygon is a back face if  $\mathbf{V}_{\text{view}} \cdot \mathbf{N} > 0$ .
- If the object has been converted to projection coordinates, then our viewing direction is parallel to the  $z$  axis and only need to consider  $z$  component of  $\mathbf{N}$ . So a polygon is a back iff the  $z$  component of  $\mathbf{N}$ ,  $C$  above, is less than 0.

# The Depth Buffer Method

- This method compares surface depth values throughout a scene for each pixel position on the projection plane.
- It works for non planar surfaces, but is usually implemented for polygon surfaces.
- Sometimes called *z-buffer method*.

# Algorithm



- Let  $\text{depthBuff}(x,y) := 1.0$ ,  $\text{frameBuff}(x,y) = \text{backndColor}$ ; //assume 1.0=far
- Process each polygon in scene one at a time.
  - for each project  $(x,y)$  pixel position of a polygon, calculate the depth  $z$ .
  - If  $z < \text{depthBuff}(x,y)$  compute surface color of that polygon, set  $\text{depthBuff}(x,y) = z$ ;
    - $\text{frameBuff}(x,y) = \text{surfColor}(x,y)$ ;

# More Algorithm

- At  $(x,y)$ , depth is calculated from the plane equation as:  $z = -(Ax+By+D)/C$ .
- We want to be able to quickly compute adjacent points on a scan-line. So given  $z$ , to calculate depth at  $(x+1, y)$  could compute  $z' = z - A/C$
- New  $x'$  values along an edge of a polygon (changing  $y$  value by  $-1$ ) given by  $x' = x - 1/m$ , where  $m$  is the slope of the line.
- For this  $x'$  get:  $z' = z + (A/m + B)/C$ .
- The above thus describes how to quickly compute along a scan line, then how to move to next line.