Problem 2. Characterize 2-regular graphs which are felicitous.

Using the same argument as Graham and Sloane [4], we have the following.

Theorem 12. *Almost all graphs are not felicitous.*

We conclude with the following conjectures:

(1) Every n-dimensional cube is felicitous.
(2) Every graph is a subgraph of felicitous graph.
(3) (Graham and Sloane) Every tree is felicitous.
(4) The graph $P_n \cup C_{2k+1}$ is felicitous for all $n \geqslant 4$.

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